## DATABASES

I

# Query Processing 

## Outline

- Main phases of Query Processing
- Expressions in relational algebra
- Operators (revisited)
- Expressions
- Equivalence of expressions
- Estimating the cost of a query
- Algorithms for processing the relational operators
- Oracle DBMS: execution plans, statistics, query hints


## Steps in Query Processing

- Compiling the query
- Syntactic analysis
- Parsing
$\square$ Parsing tree
- Semantic analysis
- Preprocessing and rewriting in RA
- Selection of the relational algebraic representation
$\square$ Logical plan
- Selection of the algorithms
$\square$ Physical plan
- Executing the physical plan



## I. Syntactic analysis

- Context-free grammar

```
<query> ::= <SFW> | (<query>)
<SFW> ::= SELECT <select_list> FROM <table_list> WHERE <where_cond>
<select_list> ::= <identifier>, <select_list> | <identifier>
<table_list> ::= <identifier>, <table_list> | <identifier >
```

- Parsing result: parsing tree

- Example of SQL grammar in BNF: http://savage.net.au/SQL/index.html


## II. Semantic analysis <br> a. Preprocessing

- Rewrite calls to views
- Verify existence of relations
- Verify existence of attributes and ambiguity
- Verify data types

If the parsing tree is valid, it is transformed into an expression in Relational Algebra (RA)

## II. Semantic analysis

b. Rewriting in RA


## II. Semantic analysis <br> b. Rewriting in RA (continued)



## II. Semantic analysis <br> c. Logical plan - optimization

SELECT Theater
FROM Movie, Schedule
WHERE
Movie.Title = Schedule.Title
AND Movie.Actor="Winger"


## 3. Another equivalent $\pi_{\text {logical plan }}$ Theater



## II. Semantic analysis

c. Logical plan - optimization (continued)


## II. Semantic analysis <br> d. Physical plan - optimization



## Operators in relational algebra (revisited)

- Six basic operators:
- Selection: $\sigma$
- Projection: П
, Union: $\cup$
- Set difference: -
- Cartesian product: $x$
- Renaming: $\rho$
- The operators act on one or two relations and generate one new relation

Selection

- r

| $A$ | $B$ | $C$ | $D$ |
| :---: | :---: | :---: | :---: |
| $\alpha$ | $\alpha$ | 1 | 7 |
| $\alpha$ | $\beta$ | 5 | 7 |
| $\beta$ | $\beta$ | 12 | 3 |
| $\beta$ | $\beta$ | 23 | 10 |

- $\sigma_{A=B \wedge D>5}(r)$

| $A$ | $B$ | $C$ | $D$ |
| :---: | :---: | :---: | :---: |
| $\alpha$ | $\alpha$ | 1 | 7 |
| $\beta$ | $\beta$ | 23 | 10 |

## Projection

- r

| $A$ | B | C |
| :---: | :---: | :---: |
| $\alpha$ | 10 | 1 |
| $\alpha$ | 20 | 1 |
| $\beta$ | 30 | 1 |
| $\beta$ | 40 | 2 |

- $\prod_{\mathrm{A}, \mathrm{C}}(r)$

| $A$ | $C$ |
| :--- | :--- | :--- |
| $\alpha$ | 1 |
| $\beta$ | 1 |
| $\beta$ | 2 |
| $\alpha$ | 1 |$\quad$| $A$ | $C$ |
| :--- | :--- |
| $\alpha$ | 1 |

## Union

r, s

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\alpha$ | 2 |
| $\beta$ | 1 |
| $r$ |  |


| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 2 |
| $\beta$ | 3 |
| $s$ |  |

p $\mathrm{r} \cup \mathrm{s}:$

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\alpha$ | 2 |
| $\beta$ | 1 |
| $\beta$ | 3 |

## Set difference

r, s

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\alpha$ | 2 |
| $\beta$ | 1 |
| $r$ | $A$ $B$ <br> $\alpha$ 2 <br> $\beta$ 3 <br> $s$  |

r-S

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\beta$ | 1 |

## Cartesian product

r,s

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\beta$ | 2 |
| $r$ |  |


| $C$ | $D$ | $E$ |
| :---: | :---: | :---: |
| $\alpha$ | 10 | $a$ |
| $\beta$ | 10 | $a$ |
| $\beta$ | 20 | $b$ |
| $\gamma$ | 10 | $b$ |
| $s$ |  |  |


| $A$ | $B$ | $C$ | $D$ | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | $I$ | $\alpha$ | 10 | $a$ |
| $\alpha$ | $I$ | $\beta$ | 10 | $a$ |
| $\alpha$ | $I$ | $\beta$ | 20 | $b$ |
| $\alpha$ | $I$ | $\gamma$ | 10 | $b$ |
| $\beta$ | 2 | $\alpha$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 20 | $b$ |
| $\beta$ | 2 | $\gamma$ | 10 | $b$ |

## Renaming

- $\rho_{X}(E)$ - returns the result of expression $E$ named as $X$
- If the result of expression E has n attributes than

$$
\rho_{x\left(A_{1}, A_{2}, \ldots, A_{n}\right)}(E)
$$

returns the result of E named as X with attributes renamed as $A_{1}, A_{2}, \ldots, A_{n}$.

## Operators composition

- $\sigma_{A=C}\left(\begin{array}{lll}r & x\end{array}\right)$

1. $r \times s$

| $A$ | $B$ | $C$ | $D$ | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | $I$ | $\alpha$ | 10 | $a$ |
| $\alpha$ | $I$ | $\beta$ | $I 0$ | $a$ |
| $\alpha$ | $I$ | $\beta$ | 20 | $b$ |
| $\alpha$ | $I$ | $\gamma$ | 10 | $b$ |
| $\beta$ | 2 | $\alpha$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 20 | $b$ |
| $\beta$ | 2 | $\gamma$ | 10 | $b$ |

2. $\sigma_{A=C}(r \times s)$

| $A$ | $B$ | $C$ | $D$ | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | $I$ | $\alpha$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 20 | $b$ |

## Expressions in relational algebra <br> -a recursive definition

- The simplest expression is a relation $r$
- Let $E_{1}$ and $E_{2}$ be expressions in RA; then, the following are also expressions in RA:
- $E_{1} \cup E_{2}$
- $E_{1}-E_{2}$
- $E_{1} \times E_{2}$
- $\sigma_{p}\left(E_{I}\right), P$ is a predicate over attributes in $E_{I}$
- $\Pi_{s}\left(E_{I}\right), S$ is a list of attributes in $E_{I}$
- $\rho_{x}\left(E_{l}\right), x$ is a new name for $E_{l}$


## Expressing queries in RA

- Loans greater than I200


$$
\sigma_{\text {amount }>1200} \text { (loan) }
$$

- Loan number for loans greater than I200

$$
\left.\prod_{\text {loan_number }}\left(\sigma_{\text {amount }}>1200 \text { (loan }\right)\right)
$$

- Name of the clients with a loan, a deposit or both
$\Pi_{\text {customer_name }}($ borrower $) \cup \prod_{\text {customer_name }}($ depositor)


## Expressing queries in RA (ctd.)

- Name for the clients having loans at the Perryridge branch
- $\Pi_{\text {customer_name }}\left(\sigma_{\text {branch_name }}=\right.$ "Perryridge" $($
$\sigma_{\text {borrower.loan_number }}=$ loan.loan_number $($ borrower $\times$ loan $\left.)\right)$ )
- $\quad \prod_{\text {customer_name }}\left(\sigma_{\text {loan.loan_number }}=\right.$ borrower.loan_number $($ $\left(\sigma_{\text {branch_name }}=\right.$ "Perryridge" $($ loan $\left.)\right) \times$ borrower $)$ )



## Expressing queries in RA (ctd.)



- Name for the clients having loans at the Perryridge branch but having no deposits
$\prod_{\text {Customer_name }}\left(\sigma_{\text {branch_name }}=\right.$ "Perryridge" $\left(\sigma_{\text {borrower.loan_number }}=\right.$ loan.loan_number $($ borrower $\times$ loan $\left.\left.)\right)\right)$
- $\prod_{\text {customer_name }}$ (depositor)


## Additional relational operators

- Set intersection
- Natural join
- Aggregation
- External join
- Theta-join
- All of them, excepting aggregation, can be expressed using basic operators


## Set intersection

r, s

| $A$ | $B$ |
| :--- | :--- |
| $\alpha$ | I |
| $\alpha$ | 2 |
| $\beta$ | $I$ |
| $r$ | $A$ $B$ <br> $\alpha$ 2 <br> $\beta$ 3$\quad$$\|c\|$ |

- $r \cap s$

| A | B |
| :---: | :---: |
| $\alpha$ | 2 |

Natural join

- r, s

| A | B | C | D |  |
| :--- | :--- | :--- | :--- | :---: |
| $\alpha$ | l | $\alpha$ | a |  |
| $\beta$ | 2 | $\gamma$ | a |  |
| $\gamma$ | 4 | $\beta$ | b |  |
| $\alpha$ | I | $\gamma$ | a |  |
| $\delta$ | 2 | $\beta$ | b |  |
| $r$ |  |  |  |  |


| B | D | E |
| :--- | :--- | :--- |
| l | a | $\alpha$ |
| 3 | a | $\beta$ |
| l | a | $\gamma$ |
| 2 | b | $\delta$ |
| 3 | b | $\in$ |
| s |  |  |

r $\mathrm{r} \nmid s$

| A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- |
| $\alpha$ | I | $\alpha$ | a | $\alpha$ |
| $\alpha$ | I | $\alpha$ | a | $\gamma$ |
| $\alpha$ | I | $\gamma$ | a | $\alpha$ |
| $\alpha$ | l | $\gamma$ | a | $\gamma$ |
| $\delta$ | 2 | $\beta$ | b | $\delta$ |

- $\prod_{r . A, r . B, r . C, r . D, s . E}\left(\sigma_{r . B=s . B} \wedge_{r . D=s . D}\left(\begin{array}{lll}r & \mathrm{X}\end{array}\right)\right)$


## Aggregation

- Functions:
- avg
- min
- max
, sum
c count
- var
- Syntax:

$$
G_{G_{1}, G_{2}, \ldots, G_{n}} \vartheta_{F_{1}\left(A_{1}\right), F_{2}\left(A_{2}\right), \ldots, F_{n}\left(A_{n}\right)}(E)
$$

- $E$ - expresion in RA
- $G_{1}, G_{2} \ldots, G_{n}$ a list of grouping attributes (may be empty)
- Every $F_{i}$ is an aggregation function
- Every $A_{i}$ is an attribute


## Aggregation Example

- $r$

| $A$ | $B$ | $C$ |
| :--- | :--- | :--- |
| $\alpha$ | $\alpha$ | 7 |
| $\alpha$ | $\beta$ | 7 |
| $\beta$ | $\beta$ | 3 |
| $\beta$ | $\beta$ | 10 |

$g_{\text {sum(c) }}(\mathrm{r})$
sum (c )

27

- Which aggregation functions may be expressed based on basic relational operators?


## Aggregation <br> Example using basic operators

- The largest balance in the account table
account

| account_number |
| :--- |
| branch_name <br> balance |

$\prod_{\text {balance }}($ account $)-\prod_{\text {account.balance }}\left(\sigma_{\text {account.balance }}<\right.$ d.balance $\left(\right.$ account $\times \rho_{d}($ account $\left.\left.)\right)\right)$

## External join

## loan

| loan_number | branch_name | amount |
| :--- | :--- | :---: |
| L-I70 | Downtown | 3000 |
| L-230 | Redwood | 4000 |
| L-260 | Perryridge | 1700 |

borrower

| customer_name | loan_number |
| :--- | :--- |
| Jones | L-I70 |
| Smith | L-230 |
| Hayes | L-I 55 |

- loan $\bowtie$ borrower (natural join)

| loan_number | branch_name | amount | customer_name |
| :--- | :--- | :---: | :--- |
| L-I70 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |

- loan $\beth \bowtie$ borrower (left external join)

| loan_number | branch_name | amount | customer_name |
| :--- | :--- | :---: | :--- |
| L-I70 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |
| L-260 | Perryridge | 1700 | null |

## External join

> right external join
loan borrower

| loan_number | branch_name | amount | customer_name |
| :--- | :--- | :---: | :--- |
| L-I70 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |
| L-I55 | null | null | Hayes |

$>$ full external join
loan $\downarrow \varliminf_{-}$borrower

| loan_number | branch_name | amount | customer_name |
| :--- | :--- | :---: | :--- |
| L-I70 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |
| L-260 | Perryridge | 1700 | null |
| L-I55 | null | null | Hayes |

## Expressing queries in RA

## more examples

- Name for the clients having both a loan and a deposit

$$
\Pi_{\text {customer_name }} \text { (borrower) } \cap \Pi_{\text {customer_name }} \text { (depositor) }
$$

- Name for the clients having a loan and the amount

$$
\left.\Pi_{\text {customer_name, Imount }} \text { (borrower } \bowtie l \text { loan }\right)
$$

- Clients having deposits at at least the two branches named Downtown and Uptown

$$
\begin{gathered}
\Pi_{\text {customer_name }}\left(\sigma_{\text {branch_name }}=\text { "Downtown" }(\text { depositor } \bowtie \text { account })\right) \cap \\
\Pi_{\text {customer_name }}\left(\sigma_{\text {branch_name }}=\text { "Uptown" }\left(\text { depositor } \bowtie_{\text {account })}\right)\right.
\end{gathered}
$$

## Equivalence of expressions Definition

- Two expresions in RA are equivalent if they generate the same set of tuples on any instance of the database
| Remember: the order of tuples is not relevant
- Obs: SQL works with multisets


## Equivalence Rules

1. selection based on conjunctions is equivalent with a sequence of selections

$$
\sigma_{\theta_{1} \wedge \theta_{2}}(E)=\sigma_{\theta_{1}}\left(\sigma_{\theta_{2}}(E)\right)
$$

2. selections are comutative

$$
\sigma_{\theta_{1}}\left(\sigma_{\theta_{2}}(E)\right)=\sigma_{\theta_{2}}\left(\sigma_{\theta_{1}}(E)\right)
$$

3. in a sequence of projections only the last one is necessary

$$
\Pi_{L_{1}}\left(\Pi_{L_{2}}\left(\ldots\left(\Pi_{L n}(E)\right) \ldots\right)\right)=\Pi_{L_{1}}(E)
$$

4. selections may be combined with the cartesian product
a. $\quad \sigma_{\theta}\left(E_{1} \times E_{2}\right)=E_{1} \bowtie{ }_{\theta} E_{2}$
b. $\sigma_{\theta 1}\left(E_{1} \bowtie{ }_{\theta 2} E_{2}\right)=E_{1} \bowtie_{\theta \mid \wedge \theta 2} E_{2}$

## Equivalence Rules

5. theta-join and natural join are commutative

$$
E_{1} \bowtie_{\theta} E_{2}=E_{2} \bowtie_{\theta} E_{1}
$$

6. natural joins are associative

$$
\left(E_{1} \bowtie E_{2}\right) \bowtie E_{3}=E_{1} \bowtie\left(E_{2} \bowtie E_{3}\right)
$$

b) theta-joins are associative with some restrictions

$$
\left(E_{1} \bowtie_{\theta 1} E_{2}\right) \bowtie_{\theta 2 \wedge \theta 3} E_{3}=E_{1} \bowtie_{\theta 1 \wedge \theta 3}\left(E_{2} \bowtie_{\theta 2} E_{3}\right)
$$

where $\theta_{2}$ involves only attributes in $E_{2}$ and $E_{3}$

## Equivalence Rules

- visualization



## Equivalence Rules

7. selection may be distributed over theta-join
a) when $\theta_{0}$ involves only attributes in $\left(E_{1}\right)$ :

$$
\sigma_{\theta 0}\left(E_{1} \bowtie_{\theta} E_{2}\right)=\left(\sigma_{\theta 0}\left(E_{1}\right)\right) \bowtie_{\theta} E_{2}
$$

b) When $\theta$ involves only attributes in $E_{1}$ and $\theta_{2}$ involves only attributes in $E_{2}$ :

$$
\sigma_{\theta 1} \wedge_{\theta 2}\left(\mathrm{E}_{1} \bigotimes_{\theta} \mathrm{E}_{2}\right)=\left(\sigma_{\theta 1}\left(\mathrm{E}_{1}\right)\right) \bowtie_{\theta}\left(\sigma_{\theta 2}\left(\mathrm{E}_{2}\right)\right)
$$

## Equivalence Rules

## 8. projection may be distributed over theta-join

a) If $\theta$ involves only attributes in $L_{1} \cup L_{2}$ :

$$
\Pi_{L_{1} \cup L_{2}}\left(E_{1} \bowtie_{\theta} E_{2}\right)=\left(\prod_{L_{1}}\left(E_{1}\right)\right) \bowtie_{\theta}\left(\prod_{L_{2}}\left(E_{2}\right)\right)
$$

b) Consider the join $E_{\mid} \bowtie_{\theta} E_{2}$

Let $L_{1}$ and $L_{2}$ be sets of attributes in $E_{1}$ and $E_{2}$, respectively
Let $L 3$ contain attributes in $E l$ involved in $\theta$, but not in $L_{1} \cup L_{2}$, Let $L_{4}$ contain attributes in $E_{2}$ involved in $\theta$, but not in $L_{1} \cup L_{2}$

$$
\Pi_{L_{1} \cup L_{2}}\left(E_{1} \bowtie_{\theta} E_{2}\right)=\Pi_{L_{1} \cup L_{2}}\left(\left(\Pi_{L_{1} \cup L_{3}}\left(E_{1}\right)\right) \bowtie_{\theta}\left(\Pi_{L_{2} \cup L_{4}}\left(E_{2}\right)\right)\right)
$$

## Equivalence Rules

9. set union and intersection are commutative

$$
\begin{aligned}
& E_{1} \cup E_{2}=E_{2} \cup E_{1} \\
& E_{1} \cap E_{2}=E_{2} \cap E_{1}
\end{aligned}
$$

10. set union and intersection are associative

$$
\begin{aligned}
& \left(E_{1} \cup E_{2}\right) \cup E_{3}=E_{1} \cup\left(E_{2} \cup E_{3}\right) \\
& \left(E_{1} \cap E_{2}\right) \cap E_{3}=E_{1} \cap\left(E_{2} \cap E_{3}\right)
\end{aligned}
$$

1।. selection may be distributed over $\cup, \cap$ and - .

$$
\sigma_{\theta}\left(E_{1}-E_{2}\right)=\sigma_{\theta}\left(E_{1}\right)-\sigma_{\theta}\left(E_{2}\right)
$$

$$
\text { similar for } \cup \text { and } \cap \text { instead of }-
$$

$$
\sigma_{\theta}\left(E_{1}-E_{2}\right)=\sigma_{\theta}\left(E_{1}\right)-E_{2}
$$

$$
\text { similar for } \cap \text { instead of }- \text {, but not for } \cup
$$

12. projection may be distributed over union

$$
\Pi_{\mathrm{L}}\left(E_{1} \cup E_{2}\right)=\left(\Pi_{\mathrm{L}}\left(E_{1}\right)\right) \cup\left(\Pi_{\mathrm{L}}\left(E_{2}\right)\right)
$$

# Logical plan optimization 

## Optimization

## Pushing selection

- Example I:
- Name of the clients having an account at the branches located in Brooklyn

$$
\Pi_{\text {customer_name }}\left(\sigma_{\text {branch_city }=\text { "Brooklyn" }}(\text { branch } \bowtie(\text { account } \bowtie \text { depositor }))\right)
$$

- Based on rule 7a obtain:

$$
\Pi_{\text {customer_name }}\left(\left(\sigma_{\text {branch_city ="Brooklyn" }}(\text { branch })\right) \bowtie(\text { account } \bowtie \text { depositor })\right)
$$

- By performing selection earlier, the size of the relations at join becomes smaller



## Optimization <br> Pushing selection

- Example 2:
- Name of the clients having an account at the branches located in Brooklyn having the balance greater than 1000
$\Pi_{\text {customer_name }}\left(\sigma_{\text {branch_city }}=\right.$ "Brooklyn" $\wedge$ balance $>1000($ branch $\bowtie($ account $\bowtie$ depositor $\left.))\right)$
- Based on rule 6a (join associativity):
$\Pi_{\text {customer_name }}\left(\left(\sigma_{\text {branch_city }}=\right.\right.$ "Brooklyn" $\wedge$ balance $>1000\left(\right.$ branch $\left.\bowtie_{\text {account })}\right) \bigwedge_{\text {depositor }}$
- Now we can perform the selection earlier:
$\sigma_{\text {branch_city }}=$ "Brooklyn" $($ branch $) \ \sigma_{\text {balance }}>1000(a c c o u n t)$


## Optimization

## Pushing selection (example 2 illustrated)


(a) Initial expression tree
(b) Tree after multiple transformations

## Optimization <br> Pushing projection

- Example

$$
\Pi_{\text {customer_name }}\left(\left(\sigma_{\text {branch_city }}=\text { "Brooklyn" }(\text { branch }) \bowtie \text { account }\right) \bowtie \text { depositor }\right)
$$

- Eliminate the attributes no longer needed:

$$
\Pi_{\text {customer_name }}\left(\left(\Pi_{\text {account_number }}\left(\sigma_{\text {branch_city }} \text { "Brookyy" }(\text { branch }) \bowtie_{\text {account })}\right) \bowtie_{\text {depositor }}\right)\right.
$$

- By performing projection in advance, the size of the relations at join becomes smaller


## Optimization <br> Ordering at join

- According to rule 6:

$$
\left(r_{1} \bowtie r_{2}\right) \bowtie r_{3}=r_{1} \bowtie\left(r_{2} \bowtie r_{3}\right)
$$

- If $r_{2} \bowtie r_{3}$ is larger than $r_{1} \bowtie r_{2}$, than choose

$$
\left(r_{1} \bowtie r_{2}\right) \bowtie r_{3}
$$

- Example
$\Pi_{\text {customer_name }}\left(\left(\sigma_{\text {branch_city }}=\right.\right.$ "Brooklyn" $($ branch $\left.)\right) \bowtie($ account $\bowtie$ depositor) $)$

Only a small number of clients have accounts at Brooklyn branch, therefore is more advantageous to execute first
$\sigma_{\text {branch_city }}$ = "Brooklyn" (branch) \account

- For $n$ relations there exist $(2(n-I))!/(n-I)$ ! different orderings for join.
- $n=7->665280, n=10->176$ bilions!

To reduce the number of orderings under consideration, dynamic programming may be used

## Cost estimation for logical plans

- $I_{r}$ : dimension of a tuple in $r$ (in bytes).
- $n_{r}$ : number of tuples in $r$.
- $b_{r}$ : number of blocks used to store $r$.
- $f_{r}$ : number of tuples in $r$ that can be stored in a block
- If the tuples of $r$ are stored in a single file (contiguous blocks on hard disk):

$$
b_{r}=\left\lceil\frac{n_{r}}{f_{r}}\right\rceil
$$

- $V(A, r)$ : number of distincst values of attribute $A$ in $r$; equivalent to the dimension of $\prod_{A}(r)$ (on sets and not multi-sets).
- The logical plan generator estimates the number of tuples/blocks which result from each relational operator in the logical plan; these estimates are further used by the physical plan generator


## Estimarea dimensiunii selecției

## $\sigma_{A=r}(\boldsymbol{r})$

( $n_{r} / V(A, r)$ : numărul de înregistrări ce satisfac selecția
> pentru atribut cheie: I
$\sigma_{A \leq V}(r)\left(c a z u l \sigma_{A \geq V}(r)\right.$ este simetric)
dacă sunt disponibile $\min (A, r)$ și max $(A, r)$

- 0 dacă $\mathrm{r}<\min (\mathrm{A}, \mathrm{r})$
$n_{r} \cdot \frac{v-\min (A, r)}{\max (A, r)-\min (A, r)} \quad$ alfel
》 dacă sunt disponibile histograme se poate rafina estimarea anterioară
> în lipsa oricărei informații statistice dimensiunea se consideră a fi $n_{r} / 2$.


## Estimarea dimensiunii selecțiilor complexe

Selectivitatea unei condiții $\theta_{i}$ este probabilitatea ca un tuplu în relația $r$ să satisfacă $\theta_{i}$
, dacă numărul de tuple ce satisfac $\theta_{i}$ este $s_{i}$, selectivitatea e $s_{i} / n_{r}$
Conjuncția (în ipoteza independenței)

Disjuncția

$$
\sigma_{\theta \mid \wedge \theta 2 \wedge \ldots \wedge \theta n}(r): \quad n_{r} * \frac{s_{1} * s_{2} * \ldots * s_{n}}{n_{r}^{n}}
$$

$\sigma_{\theta 1 \vee \theta^{2} \vee \ldots \vee \theta_{n}}(r)$ :

$$
n_{r} *\left(1-\left(1-\frac{s_{1}}{n_{r}}\right) *\left(1-\frac{s_{2}}{n_{r}}\right) * \ldots *\left(1-\frac{s_{n}}{n_{r}}\right)\right)
$$

Negația

$$
\sigma_{-\theta}(r): \quad n_{r}-\operatorname{size}\left(\sigma_{\theta}(r)\right)
$$

## Estimarea dimensiunii joinului

pentru produsul cartezian $r \times s$ : $n_{r} * n_{s}$ tuple, fiecare tuplu ocupă $s_{r}+s_{s}$ octeți
pentru $r \bigotimes_{s}$
) $R \cap S=\varnothing: n_{r}{ }^{*} n_{s}$
) $R \cap S$ este $\circ$ (super)cheie pentru $R:<=n_{s}$
> $R \cap S=\{A\}$ nu e cheie pentru $R$ sau $S: \frac{n_{r} * n_{s}}{V(A, s)}$ sau $\frac{n_{r} * n_{s}}{V(A, r)}$
> minimul este considerat de acuratețe mai mare
> dacă sunt disponibile histograme se calculează formulele anterioare pe fiecare celulă pentru cele două relații

## Estimarea dimensiunii pentru alte operații

Proiecția $\Pi_{A}(r): V(A, r)$
Agregarea: ${ }_{A} \boldsymbol{g}_{\mathrm{F}}(r): V(A, r)$
Operațiii pe mulț̦imi
, rus: $\mathrm{n}_{\mathrm{r}}+\mathrm{n}_{\mathrm{s}}$
, $r \cap s: \min \left(n_{r}, n_{s}\right)$
, r-s:n $n_{r}$
Join extern
, r $\beth$ s: $\operatorname{dim}(r \quad s)+n_{r} \quad \bowtie$

- $r \npreceq s=\operatorname{dim}(r \quad s)+n_{r}+n_{s} \bowtie$
$\sigma_{\theta 1}(r) \cap \sigma_{\theta 2}(r)$ echivalent cu $\sigma_{\theta 1} \sigma_{\theta 2}(r)$

Estimatorii furnizează în general margini superioare

# Physical plan optimization 

## Estimating costs for physical plans

- The cost is generally measured as the time needed to return the result
- Disk access is considered to be the most costly operation
- Number of seeks ${ }^{*} t_{s}$ (time to localize a single data block)
- Number of blocks read/written $* t_{T}$ (transfer time)
- CPU cost is ignored for simplicity
- The cost for transferring $b$ data blocks which required $S$ seeks:

$$
b * t_{T}+S * t_{S}
$$

## Algorithms for selection

- Linear search (full scan)
${ }^{\nu}$ cost: $b_{r} * t_{T}+t_{S}$
b if selection is over a key attribute, estimated cost: $b_{r} / 2 * t_{T}+t_{S}$
- may be applied for any search condition, data file ordering, existence of indexes
- Binary search
- Applicable for equality conditions on the sort key
- The cost of finding one qualifying tuple: $\left\lceil\log _{2}\left(b_{r}\right)\right\rceil *\left(t_{T}+t_{\mathrm{s}}\right)$;

If there exist several qualifying tuples only transfer time is added

- Index scan (suppose a B+-tree exists for the search key)
> primary index on a candidate key, equality cond.: $\left(h_{i}+I\right) *\left(t_{T}+t_{S}\right)$
> primary index on a none-key, equality cond.: $h_{i} *\left(t_{T}+t_{S}\right)+t_{S}+t_{T} * \mathrm{~b}$
> secondary index, equality, n tuples returned: $\left(h_{i}+n\right) *\left(t_{T}+t_{\mathrm{s}}\right)$
$>$ primary index, range cond.: $h_{i} *\left(t_{T}+t_{S}\right)+t_{S}+t_{T} * b$
, secondary index, range cond: ?


## Algorithms for complex selections

- Conjunction: $\sigma_{\theta 1} \wedge{ }_{\theta 2} \wedge \ldots{ }_{\theta n}(r)$
- Use an index for $\theta_{\text {l }}$ and verify the rest when bringing data into memory
- Use a multi-key index
- Intersect the set of pointers returned by searching over all the indexes
- Disjunction: $\sigma_{\theta 1} \vee{ }_{\theta 2} \vee \cdots{ }_{\theta n}(r)$
- Union of the set of identifiers returned by index searches


## Algorithms for join

- Algorithms:
, nested-loop join
- indexed nested-loop join
- merge join
- hash join
- Choosing from above implies cost estimation - requires estimates for the logical plan


## Nested-loop joins

- For a theta-join: $r \bowtie_{\theta} s$ :
for each tuple $t_{r}$ in $r$ do begin
for each tuple $t_{s}$ in $s$ do begin
if $\left(t_{p} t_{s}\right)$ satisfies $\theta$
add $t_{r} \cdot t_{s}$ to the result set
end
end
- Inner relation - s
- External relation - r
- Estimated cost: $\left(n_{r} * b_{s}+b_{r}\right) * t_{T}+\left(n_{r}+b_{r}\right) * t_{s}$
- May be used for any join condition


## Indexed nested-loop join

- Full file scans may be replaced by index scans if:
- we deal with an equi-join (as a special case natural join)
- there exists an index for the inner relation associated to the join attribute
- Idea: for every tuple $t_{r}$ in $r$ use the index to retrieve all the tuples in $s$ satisfying the join condition equivalent to a selection on $s$ with the join condition
- Cost: $b_{r}\left(t_{T}+t_{S}\right)+n_{r} * c$
- c is the cost of index search
- if indexes for both relations are available, the relation with fewer tuples will be used as external within join
- Example:
- depositor $\nVdash$ customer, depositor external relation
- customer has a primary index of type $\mathrm{B}^{+}$-tree on the join attribute customer-name, with $\mathrm{m}=20$ entries per node
- customer: 10,000 tuples ( $\mathrm{f}=25$ ), depositors:5000 tuples ( $\mathrm{f}=50$ )
- cost: $100+5000 * 5=25,100$ blocks transferred and seeks (compare to the case of standard nested-loop join: $2,000,100$ blocks transferred and $=5100$ seeks)


## Merge join

- May be used only for equi-joins
- Algorithm:

Sort both relations based on the join attributes (luckily, they are stored ordered)
Merge the two relations

## Cost:

- $b_{r}+b_{s}$ transferred blocks
+ the cost of sorting


## Hybrid merge join:

- one relation is sorted, while for the second a B+ -tree associated to the join attribute is used
- The sorted relation merges with the leaf level of the tree


## Hash Join

- Applicable only for echi-join
- Algorithm: a hash function $h$ aplied on the join attribute is used to partition the tuples of both relations into data blocks that fit in the main memory:
- $r_{1}, r_{2}, \ldots r_{n}$
${ }^{*} s_{1}, s_{2}, \ldots s_{n}$
- tuples in $r_{i}$ are compared only with tuples $s_{i}$



## Complex joins

- Conjunction of conditions: $r \rrbracket_{\theta \mid \wedge \theta 2 \wedge \ldots \wedge \theta} s$
, Nested-loop join, verify all the conditions
- Compute a simpler join $r \bigwedge_{\theta i} s$ and afterwards verify the rest of conditions

- Nested-loop join, start verifying the conditions until one is satisfied
- Compute the union of individual joins (applicable only for the set version of union)
$\left(r \bigwedge_{\theta 1} s\right) \cup\left(r \bigotimes_{\theta 2} s\right) \cup \ldots \cup\left(r \bigotimes_{\theta n} s\right)$


## Eliminating duplicates

- Based on sorting or hashing
- Because is costly, DBMSs eliminate tuples only when explicitly asked


## Evaluating RA expressions (executing physical plans)

- The operators in the RA expression/tree are evaluated starting with the last level and moving up to the root
- Versions:
- Materialize: (sub)expressions on lower levels are materialized as new relations (as data files stored on disks) and are given as entries for upper levels
- Pipelining: tuples are given as entries to the operators on the upper levels when they are generated
$\square$ Not always possible (think of hash join over merge join)
, Consumer based: the upper level asks for new tuples
- Producer based: the operator on the lower level writes in buffer and the parrent takes from the buffer (when the buffer is full there are waiting times on the lower level)


## Inspecting execution plans in Oracle

- Record the plan:

EXPLAIN PLAN
[SET STATEMENT_ID = <id>]
[INTO <table_name>]
FOR <sql_statement>;

- Possible for any DML statement
- Visualizing the plan:

SELECT * FROM table(dbms_xplan.display);
or (not so nicely formatted)
select * from plan_table [where statement_id = <id>];
http://www.oracle.com/technetwork/database/bi-datawarehousing/twp-explain-the-explain-plan-05201I-
393674.pdf

## Execution plans in Oracle

## Statistics

- Table statistics
- Number of rows
- Number of blocks
> Average row length
- Column statistics
- Number of distinct values (NDV) in column
- Number of nulls in column
- Data distribution (histogram)
- Index statistics
- Number of leaf blocks
- Levels
- Clustering factor
- System statistics
- I/O performance and utilization
- CPU performance and utilization


## Execution plans in Oracle Collecting statistics

- Procedures in package DBMS_STATS:
- GATHER_INDEX_STATS
- Index statistics
- GATHER_TABLE_STATS

Table, column, and index statistics

- GATHER_SCHEMA_STATS
- Statistics for all objects in a schema
- GATHER_DATABASE_STATS
- Statistics for all objects in a database
- GATHER_SYSTEM_STATS
- CPU and I/O statistics for the system
- http://docs.oracle.com/cd/BI0500_0l/server.920/a96533/stats.htm


## Execution plans in Oracle Hints

- When launching a query it is possible to indicate the Oracle optimizer some choices for the execution plan:

SELECT /*+ USE_MERGE(employees departments) */* FROM employees, departments WHERE employees.department_id = departments.department_id;
http://docs.oracle.com/cd/BI9306_01/server.I02/bI4200/sql_elements006.htm

## References

- ChaptersI 3 and I4 in Avi Silberschatz Henry F. Korth S. Sudarshan. "Database System Concepts". McGrawHill Science/Engineering/Math; 4th edition

